Inference at $*$ 2 0 0 0
of proof for Lemma before_last:

1. T : Type
2. T List
3. u : T
4. v : T List
5. $\forall x{:}T.\ (x \in v) \Rightarrow (\neg(x = \text{last}(v))) \Rightarrow x$ before $\text{last}(v) \in v$

$\vdash \forall x{:}T.\ (x \in [u\ /\ v]) \Rightarrow (\neg(x = \text{last}([u\ /\ v]))) \Rightarrow x$ before $\text{last}([u\ /\ v]) \in [u\ /\ v]$
by PERMUTE{1:n,
1:n,
2:n,
3:n,
4:n,
5:n,
5:n,
6:n,
7:n,
8:n,
9:n,
9:n,
10:n,
11:n,
12:n,
13:n,
14:n,
15:n,
16:n,
17:n,
1:n,
18:n}

1: . . . . .wf. . . . . NILNIL

$\vdash T \in$ Type
2: . . . . .wf. . . . . NILNIL

$\vdash (\lambda x.(x \in [u\ /\ v]) \Rightarrow (\neg(x = \text{last}([u\ /\ v]))) \Rightarrow [x;\ \text{last}([u\ /\ v])] \subseteq [u\ /\ v])$
$\in T \rightarrow \mathbb{P}$
3: . . . . .wf. . . . . NILNIL

$\vdash (\lambda x.(x \in [u\ /\ v])$
$\Rightarrow (\neg(x = \text{last}([u\ /\ v])))$
$\Rightarrow ((x = u\ \&\ [\text{last}([u\ /\ v])] \subseteq v) \vee [x;\ \text{last}([u\ /\ v])] \subseteq v))$

$\in T \to \mathbb{P}$
4: . . . . .wf. . . . . NILNIL

$\vdash T = T$
5: . . . . .wf. . . . . NILNIL

6. $x : T$
$\vdash (x \in [u \ / \ v]) \in \mathbb{P}$
6: . . . . .wf. . . . . NILNIL

6. $x : T$
$\vdash ((\neg(x = \text{last}([u \ / \ v]))) \Rightarrow [x; \text{last}([u \ / \ v])] \subseteq [u \ / \ v]) \in \mathbb{P}$
7: . . . . .wf. . . . . NILNIL

6. $x : T$
$\vdash ((\neg(x = \text{last}([u \ / \ v])))$
$\Rightarrow ((x = u \ \& \ [\text{last}([u \ / \ v])] \subseteq v) \vee [x; \text{last}([u \ / \ v])] \subseteq v))$
$\in \mathbb{P}$
8: . . . . .wf. . . . . NILNIL

6. $x : T$
$\vdash (x \in [u \ / \ v]) = (x \in [u \ / \ v])$
9: . . . . .wf. . . . . NILNIL

6. $x : T$
$\vdash (\neg(x = \text{last}([u \ / \ v]))) \in \mathbb{P}$
10: . . . . .wf. . . . . NILNIL

6. $x : T$
$\vdash [x; \text{last}([u \ / \ v])] \subseteq [u \ / \ v] \in \mathbb{P}$
11: . . . . .wf. . . . . NILNIL

6. $x : T$
$\vdash ((x = u \ \& \ [\text{last}([u \ / \ v])] \subseteq v) \vee [x; \text{last}([u \ / \ v])] \subseteq v) \in \mathbb{P}$
12: . . . . .wf. . . . . NILNIL

6. $x : T$
$\vdash (\neg(x = \text{last}([u \ / \ v]))) = (\neg(x = \text{last}([u \ / \ v])))$
13: . . . . .wf. . . . . NILNIL

6. T
$\vdash T \in \text{Type}$
14: . . . . .wf. . . . . NILNIL

6. $x : T$
$\vdash x \in T$

15: . . . . .wf. . . . . NILNIL

6. T
$\vdash u \in T$
16: . . . . .wf. . . . . NILNIL

6. T
$\vdash [\text{last}([u\ /\ v])] \in (T\ \text{List})$
17: . . . . .wf. . . . . NILNIL

6. T
$\vdash v \in (T\ \text{List})$
18:

$\vdash \forall x{:}T.$
$(x \in [u\ /\ v])$
$\Rightarrow (\neg(x = \text{last}([u\ /\ v])))$
$\Rightarrow ((x = u\ \&\ [\text{last}([u\ /\ v])] \subseteq v) \vee [x;\ \text{last}([u\ /\ v])] \subseteq v)$
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http://www.nuprl.org/FDLcontent/p0_963683_/p122_89337_{before_last}2_0_0_0.html